





## Representations Can be Chosen to Share Hardware

Imagine a device that performs addition on two bit patterns of an **unsigned** representation.



Can we use the same "adder" device for signed numbers? Yes! If we choose the right representations.

## Add Unsigned Bit Patterns Using Base 2 Addition

Recall that the unsigned representation is drawn from base 2.

We use base 2 addition for unsigned patterns.

Like base 10, we add digit by digit.
Unlike base 10, the single-digit table of sums is quite small...
What is 1 + 1 + 1? 11

Α	В	Sum
0	0	0
0	1	1
1	0	1
1	1	10





Unsigned Addition is Always Correct Mod $2^N$ Let SUM <sub>N</sub> (A,B) be the number represented by the sum of two N-bit unsigned bit patterns. If no overflow occurs (A + B < $2^N$ ), we have SUM <sub>N</sub> (A,B) = A + B. For sums that produce an overflow, the bit pattern of the sum is missing the $2^N$ bit, so SUM <sub>N</sub> (A,B) = A + B - $2^N$ In both cases, (SUM <sub>N</sub> (A,B) = A + B) mod $2^N$ .	Modular Arithmetic Key to Good Integer Representations Modular arithmetic is the key. It allows us to define • a representation for signed integers • that uses the same devices • as are needed for unsigned arithmetic. The representation is called 2's complement. Details soon
$(SUM_N(A,B) = A + B) \mod 2^N.$	
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