ECE 120 Second Midterm Exam
Spring 2016
Tuesday, March 15, 2016


- Be sure that your exam booklet has 8 pages.
- Write your name, netid and check discussion section on the title page.
- Do not tear the exam booklet apart.
- Use backs of pages for scratch work if needed.
- This is a closed book exam. You may not use a calculator.
- You are allowed one handwritten $8.5 \times 11$ " sheet of notes (both sides).
- Absolutely no interaction between students is allowed.
- Clearly indicate any assumptions that you make.
- The questions are not weighted equally. Budget your time accordingly.
- Show your work.

Problem 120 points
Problem 219 points
$\qquad$

Problem 318 points
$\qquad$
Problem 318 points $\qquad$
Problem 414 points $\qquad$
Problem 517 points $\qquad$
Problem 612 points $\qquad$

Total $\quad 100$ points $\qquad$

## Problem 1 (20 points): CMOS and Boolean properties

1. (5 points) Circle the correct choice for each statement. The inputs are inverted.

a. The output $Z$ equals:
$P$ AND Q PORQ PNOR Q P XOR Q P XNOR Q
b. This example best illustrates the Boolean property:

DeMorgan's Absorption No-Name Consensus
2. (15 points) Let $G(x, y, z)$ and $H(x, y, z)$ be the 3 -variable functions whose K -maps are given below.
$G(x, y, z)$

|  | yz |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 00 | 01 | 11 | 10 |
| 0 | 0 | 1 | 1 | 0 |
| 1 | 0 | 1 | 0 | 0 |

$H(x, y, z)$

|  | $\begin{array}{lllll}00 & 01 & 11 & 10\end{array}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 0 |

a. Express $H(x, y, z)$ in canonical POS form
i. Using the variables $x, y, z$ :
$H(x, y, z)=$
ii. Using the maxterm $\mathbf{M}_{\mathbf{i}}$ notation:
$H(x, y, z)=$
b. Using your expression for $H$ from part a.i), give the exact dual of $\mathbf{H}$ :
dual of $H(x, y, z)=$ $\qquad$
c. Complete the K-map (below) for function $F$, so that $F+\boldsymbol{G}=\boldsymbol{H}$. You must use don't cares wherever possible.


## Problem 2 (19 points): Sequential logic

1. (10 points) Consider the sequential feedback circuit shown below.

a. Complete the next-state table for this circuit

| $\mathbf{M}$ | $\mathbf{N}$ | $\mathbf{Q}^{+}$ |
| :---: | :---: | :---: |
| 0 | 0 | Forbidden |
| 0 | 1 |  |
| 1 | 0 |  |
| 1 | 1 |  |

b. Express the next state $Q^{+}$as a function of $M, N$, and $Q$ in SOP form.

$$
\mathrm{Q}^{+}=
$$

$\qquad$
2. (9 points) Consider a 3-bit shift register that has the following diagram:

a. Determine the functionality of the register by completing the following table

| $F_{1}$ | $F_{0}$ | Operation |
| :---: | :---: | :---: |
| 0 | 0 | Unused |
| 0 | 1 |  |
| 1 | 0 |  |
| 1 | 1 |  |

b. If the shift register initially stores $Q_{2} Q_{1} Q_{0}=100$ and Input=0, what is stored in the register after one clock pulse and
$F_{1} F_{0}=01 ?$ $\qquad$
$F_{1} F_{0}=10 ?$ $\qquad$ (Assume again that 100 is stored before the operation.)
$F_{1} F_{0}=11 ?$ $\qquad$ (Assume again that 100 is stored before the operation.)

## Problem 3 (18 points)

Consider the 4 -variable function $f(w, x, y, z)$, with the following K-map (drawn twice).
minimal SOP
yz



1. Give a minimal SOP expression for $f(w, x, y, z)$ and show the corresponding loops on the left map.
min SOP: $\qquad$
2. Give a minimal POS expression for $f(w, x, y, z)$ and show the corresponding loops on the right map.
min POS: $\qquad$
3. Implement $f$ using only a 4:1 multiplexer (with select inputs $\mathrm{S}_{1} \mathrm{~S}_{0}=w x$ ) and one NAND gate. Complemented inputs are not available.


## Problem 4 (14 points)

In this problem you will complete the design of the circuit shown below, which compares two 4 -bit unsigned binary numbers $A=a_{3} a_{2} a_{1} a_{0}$ and $B=b_{3} b_{2} b_{1} b_{0}$ and outputs

$$
f=\left\{\begin{array}{cc}
x \text { NAND } y & \text { if } A<B \\
x^{\prime} O R y & \text { if } A \geq B
\end{array}\right.
$$



1. (8 points) Design cell $C$ so that the comparator portion of the above circuit operates correctly and outputs

$$
c_{4}= \begin{cases}0 & \text { if } A<B \\ 1 & \text { if } A \geq B\end{cases}
$$

a. Specify the input $\mathrm{c}_{0}$.
$\mathrm{C}_{0}=$ $\qquad$
b. Express $c_{i+1}$ in terms of $c_{i}, a_{i}, b_{i}$.
$c_{i+1}=$ $\qquad$
2. (6 points) Design the network N by giving a Boolean expression for f .
$\mathrm{f}=$ $\qquad$

## Problem 5 (17 points)

Shown below is an 8-bit arithmetic unit (AU) which operates on two 8-bit 2's complement numbers A and B . Each network N computes $\mathrm{a}^{*}$ and $\mathrm{b}^{*}$, where:

$$
\begin{aligned}
& a^{*}=k_{1}{ }^{\prime} k_{0}{ }^{\prime}+k_{1} a \\
& b^{*}=k_{1} k_{0}{ }^{\prime} b^{\prime}+k_{0} b+k_{1}{ }^{\prime} k_{0}{ }^{\prime} a
\end{aligned}
$$



1. (4 points) Give a 2-level NAND gate implementation of $a^{*}$. Assume complemented inputs are available.
2. (13 points) Complete the table below.
a. Give the values for $a^{*}, b^{*}, c_{0}$
b. Specify the operation performed. Express your answer as an arithmetic function (PLUS/MINUS) of A and B (e.g., "a plus the complement of b" is not an appropriate response).

| $\mathbf{k}_{1}$ | $\mathbf{k}_{0}$ | $\mathbf{a}^{*}$ | $\mathbf{b}^{*}$ | $\mathbf{c}_{0}$ | Operation performed as a function of A and B <br> $($ e.g. A PLUS/MINUS B) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 |  |  |  |  |
| 0 | 1 |  |  |  |  |
| 1 | 0 |  |  |  |  |
| 1 | 1 |  |  |  |  |

## Problem 6 (12 points): Finite State Machines

The circuit below is a 2-bit register that shifts right with serial input of 0 when $K=0$ and parallel loads with inputs of 1 when $K=1$.


1. ( 6 points) Complete the state transition table for the circuit.

| $S_{1}$ | $S_{0}$ | $K$ | $S_{1}^{+}$ | $S_{0}^{+}$ | $Z$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 0 |  |  |  |
| 0 | 0 | 1 |  |  |  |
| 0 | 1 | 0 |  |  |  |
| 0 | 1 | 1 |  |  |  |
| 1 | 0 | 0 |  |  |  |
| 1 | 0 | 1 |  |  |  |
| 1 | 1 | 0 |  |  |  |
| 1 | 1 | 1 |  |  |  |

2. (6 points) Complete the state transition diagram for the circuit.


## Boolean algebra properties



Feel free to tear this page off and use it as scratch paper.

