## ECE 198JL Final Exam

Spring 2013
May 9 ${ }^{\text {th }}, 2013$

| Name: |  |  |
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| Discussion Section: |  |  |

- Be sure your exam booklet has 10 pages.
- Be sure to write your name and lab section on the first page.
- Do not tear the exam booklet apart.
- We have provided LC-3 instructions set and other reference materials on separate pages.
- Use backs of pages for scratch work if needed.
- This is a closed book exam. You may not use a calculator.
- You are allowed two handwritten $8.5 \times 11$ " sheets of notes.
- Absolutely no interaction between students is allowed.
- Be sure to clearly indicate any assumptions that you make.
- The questions are not weighted equally. Budget your time accordingly.
- Don't panic, and good luck!

Problem 118 points: $\qquad$
Problem 212 points: $\qquad$

Problem 310 points: $\qquad$
Problem 410 points: $\qquad$
Problem 58 points: $\qquad$
Problem 610 points: $\qquad$
Problem 710 points: $\qquad$
Problem 822 points: $\qquad$

Total 100 points: $\qquad$

## Problem 1 (18 pts): LC-3 microinstructions

You are adding a new instruction, called $\mathbf{C P}$, to the LC-3 instruction set. This instruction copies a value from one memory location whose address is stored in the register specified by $\operatorname{IR}[11: 9]$ to another memory location whose address is specified as a PC-relative offset by IR[8:0]. The binary encoding of this new instruction is as follows:

a) In RTL form, give a sequence of (at most 4) microinstructions that implement the execute phase of the CP instruction. Make sure your implementation does not modify any values in the general-purpose register file.
b) The execute phase of $\mathbf{C P}$ instruction starts at control ROM address $\qquad$ (answer in binary with the correct number of bits).
c) Determine control ROM microinstructions that implement the RTL statements from part (a). Complete the table below by filling in 0,1 , or x as appropriate. Use don't cares wherever possible. Specify ROM addresses in decimal. When you need additional states, state numbers $\mathbf{5 5}, \mathbf{5 6}, \mathbf{5 7}$, and $\mathbf{5 8}$ are available for your use.

|  | ¢ | $\begin{aligned} & \widehat{ } \\ & \underset{O}{\delta} \\ & 0 \end{aligned}$ | ${ }_{0}^{6}$ |  |  |  |  |  | $\begin{aligned} & \overparen{\sim} \\ & \sum_{n}^{N} \\ & \stackrel{\sim}{n} \\ & \underset{\sim}{\sim} \end{aligned}$ | ¢ | $$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | Do not fill in this space. <br> Only fill in control word bits for the first two microinstructions. |  |  |  |  |  |  |  |

d) We could have accomplished the task of copying a value from one memory location to another memory location by simply writing a short program using existing instructions. Write such a program in LC-3 assembly language assuming that the memory source address is stored in R6 and the memory destination address is labeled as DEST.
a) On the LC-3 datapath shown on the right, highlight two different paths that can be used to implement the following RTL statement: PC $\leftarrow$ SR1 where SR1 is specified by IR [8:6]. For each path, write down GATE and MUX control signals below. Use don't cares when possible.

## Path 1

GateMARMUX: $\qquad$
GateMDR: $\qquad$
GateALU: $\qquad$
GatePC: $\qquad$
MARMUX: $\qquad$
PCMUX(2): $\qquad$
ADDR1MUX: $\qquad$
ADDR2MUX(2): $\qquad$
DRMUX(2): $\qquad$
SR1MUX(2): $\qquad$
ALUK(2): $\qquad$

## Path 2

GateMARMUX: $\qquad$
GateMDR: $\qquad$
GateALU: $\qquad$
GatePC:
MARMUX: $\qquad$
PCMUX(2): $\qquad$
ADDR1MUX: $\qquad$
ADDR2MUX(2): $\qquad$
DRMUX(2): $\qquad$
SR1MUX(2): $\qquad$
ALUK(2): $\qquad$

b) Give the RTL for the following control word, based on the LC-3 architecture. Do not use terms like 'SR' or 'DR'; use the specific IR bits by name (e.g. IR[11:9] instead of DR).

## Problem 3 (10 pts): LC-3 assembly program analysis

The following program counts occurrence of a character in a file. Character to count is input from the keyboard. The count (which must be < 9) is shown on the display. File starts in memory from address x3016 and is terminated by the EOT ASCII control character (EOT's ASCII value is $x 4$ ).
a) Fill in missing instructions

|  | . ORIG | x3000 |
| :---: | :---: | :---: |
|  | AND | R2, R2, \#0 |
|  | LD | R3, PTR |
|  | IN |  |
| NEXT | LDR | R1, R3, \#0 |
|  | BRz | OUTPUT |
|  | NOT | R1, R1 |
|  | ADD | R1, R1, \#1 |
|  | ADD | R4, R1, R0 |
|  | ADD | R2, R2, \#1 |
| SKIP | ADD | R3, R3, \#1 |
|  | BRnzp | NEXT |
| OUTPUT | LD | R0, ASCII |
|  | OUT |  |
|  | HALT |  |
| ASCII | .FILL | x0030 |
| PTR | .FILL | x3016 |
|  | . END |  |

b) Draw flowchart for the above program. Be specific, use standard symbols only (ovals, rhombs, rectangles, etc.) The flowchart is already partially built to give you an example of what's expected.

c) Complete the symbol table for the above program.

| Symbol Name | Address |
| :---: | :---: |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |

d) Briefly explain why the count must be $<9$.

## Problem 4 (10 pts): LC-3 assembly language programming

Write a program that computes max of 2 integer numbers. The numbers are stored in memory locations labeled as NUM1 and NUM2. The result should be stored in memory location labeled as RES.
a) Draw flowchart
 for the solution to the above problem.
b) Write a program in LC-3 assembly language that corresponds to the above flowchart. The program must start at memory address x4000. The two values must be initialized to 10 and -20 . The program must terminate and it must be well-documented such that it can be graded by a human.

## Problem 5 (8 pts): ALU

The ALU below has control signals $k_{2} k_{1} k_{0}$. It takes two 16 -bit input words $A=a_{15} \ldots a_{0}$ and $B=b_{15} \ldots b_{0}$ and produces a 16 -bit output word $F=f_{15} \ldots f_{0}$. The combinational circuit $M$ produces modified adder inputs $A^{*}=a_{15}{ }^{*} \ldots a_{0} *$ and $B^{*}=$ $b_{15}{ }^{*} \ldots b_{0}{ }^{*}$. The Logic Unit produces $H=h_{15} \ldots h_{0}$.

| $k_{2}$ | $k_{1}$ | $k_{0}$ | $F$ |
| :---: | :---: | :---: | :---: |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | $A$ plus $B$ |
| 0 | 1 | 0 | $B$ plus 1 |
| 0 | 1 | 1 | $B$ minus 1 |
| 1 | 0 | 0 | $A$ |
| 1 | 0 | 1 | $B$ |
| 1 | 1 | 0 | $\operatorname{not} B$ |
| 1 | 1 | 1 | $A$ and $B$ |


a) Using these Karnaugh maps, define the modified adder inputs $a_{i}{ }^{*}$ and $b_{i}{ }^{*}$ and the logic unit outputs $h_{i}$. Also write the simplest possible Boolean expression for $c_{0}$, the carry-in to the adder.


$$
c_{0}=
$$

b) The adder also produces one-bit status signals $V, N$, and $Z$. Write Boolean expressions for these signals as functions of $g_{i}$ and $c_{i}$.
$V=1$ in case of overflow: $V=$
$N=1$ if the result is negative: $N=$ $\qquad$
$Z=1$ if the result is $0: Z=$ $\qquad$

## Problem 6 (10 pts): Next-instruction unit design

You are designing a next-generation computer called NextGen198jl. Among other things, this computer has the nextinstruction unit that decides what the PC's next value should be. For jumps, the PC should be loaded with the zeroextended target address specified in the instruction (PC $\leftarrow \operatorname{ZEXT}(\operatorname{IR}[11: 0])$ ). For branch instructions, the PC should be loaded with the updated target address only if the corresponding status bit ( N for negative or Z for zero) is true (if N \& IR[10] or $\mathrm{Z} \& \operatorname{IR}[9]$, then $\mathrm{PC} \leftarrow \mathrm{PC}+\mathrm{SEXT}(\operatorname{IR}[8: 0]$ ), otherwise $\mathrm{PC} \leftarrow \mathrm{PC}+1$ ). For all other instructions, the PC should just be incremented by 1 ( $\mathrm{PC} \leftarrow \mathrm{PC}+1$ ). Formats of JUMP and BRANCH instructions are shown below. Note that the opcodes in NextGen198jl ISA are 5-bit long.

JUMP


## BRANCH


a) Write Boolean expression for JMP as a function of OPCODE. JMP $=1$ when IR[15:11]=11010.
$\mathrm{JMP}=$ $\qquad$
b) Write Boolean expression for BEN. BEN = 1 when IR holds BRANCH instruction and the corresponding status bit ( N or Z ) is true.

BEN $=$ $\qquad$
c) Complete the implementation of the next-instruction unit below. You can only use one adder (ADD), one zero extension unit (ZEXT), one sign extension unit (SEXT), one increment-by-one unit ( +1 ), one MUX (already drawn), and as few additional gates as possible. You can size all the units/gates as needed. Use signals JMP and BEN from parts (a) and (b) to control the MUX. Label all components and signals properly. E.g., IR[15:11] can be used to label wires that carry opcode of the instruction. Excessive complexity will be penalized.


## Problem 7 (10 pts): Boolean algebra and combinational circuits

a) From the circuit shown on the right, write Boolean expression for H .
$\mathrm{H}=$ $\qquad$
b) Express H in minimal SOP form.
$\mathrm{H}=$ $\qquad$
c) Express H in minimal POS form.
$\mathrm{H}=$ $\qquad$

d) Draw two-level AND-to-OR network and two-level NOR-NOR network for H. Assume that inverted inputs are available.

| AND-OR | NOR-NOR |
| :--- | :--- |
|  |  |

e) Explain advantages of implementing circuits as two-level AND-to-OR or OR-to-AND networks.
f) Explain advantages of implementing circuits as two-level NAND-to-NAND or NOR-to-NOR networks when using CMOS technology.

## Problem 8 (22 pts): Sequential circuits and FSM

You are designing a vending machine. The machine sells jawbreaker candy for $25 \phi$. The machine accepts $N$ (nickels $=$ $5 \phi), D($ dimes $=10 \phi)$, and $Q$ (quarters $=25 \phi)$ coins only. When the sum of the coins inserted in sequence is $25 \phi$ or more, the machine dispenses one jawbreaker by asserting $D J$ output signal and returns to its initial state. No change is returned. $D J=0$ in all other states. If anything less than $25 ¢$ is inserted and the Coin Return ( $C R$ ) pushbutton is pushed ( $C R=1$ ), the coins deposited so far are returned by asserting $R C$ output signal, after which the machine returns back to its initial state. $C R=0$ in all other states.
a) Draw Moore state diagram for this FSM below. Assign states (you will need this for part (b)). Make sure to label each state with name and output and each edge with input. Make sure to label all parts, inputs, outputs, edges, etc. Points will be deducted for missing labels and messy drawing.
b) Based on the above FSM and your state assignments, show the next-state table for your initial state only. (Remember, only one coin can be inserted at a time, therefore your next-state table should be fairly short.)
c) Implement the above FSM using negative-edge triggered D flip-flops. Do not implement the actual next-state and output logic; instead just draw boxes representing the circuits that compute next-state bits as functions of current state and external inputs, and outputs as functions of current state only. Make sure to label all parts, inputs, and outputs. Points will be deducted for missing labels and messy drawing.

